



Intro to Glauber Model

Modeling the experimental observables to determine centrality.

UCDAVIS
DEPARTMENT OF PHYSICS

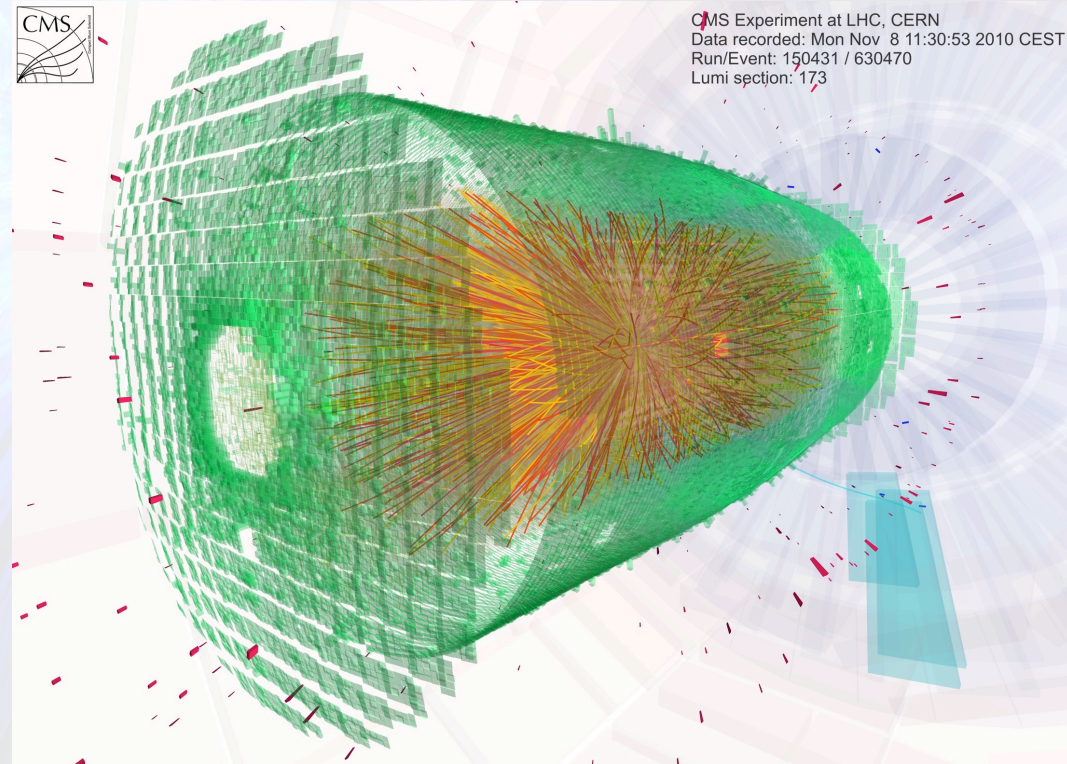
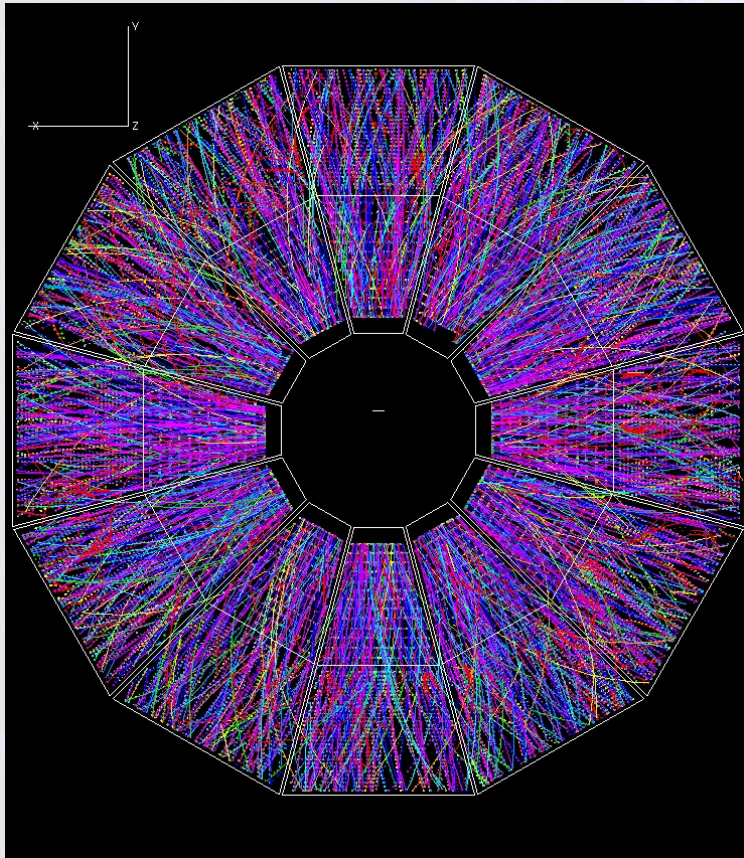


Manuel Calderón de la Barca Sánchez



Calculate particle multiplicity

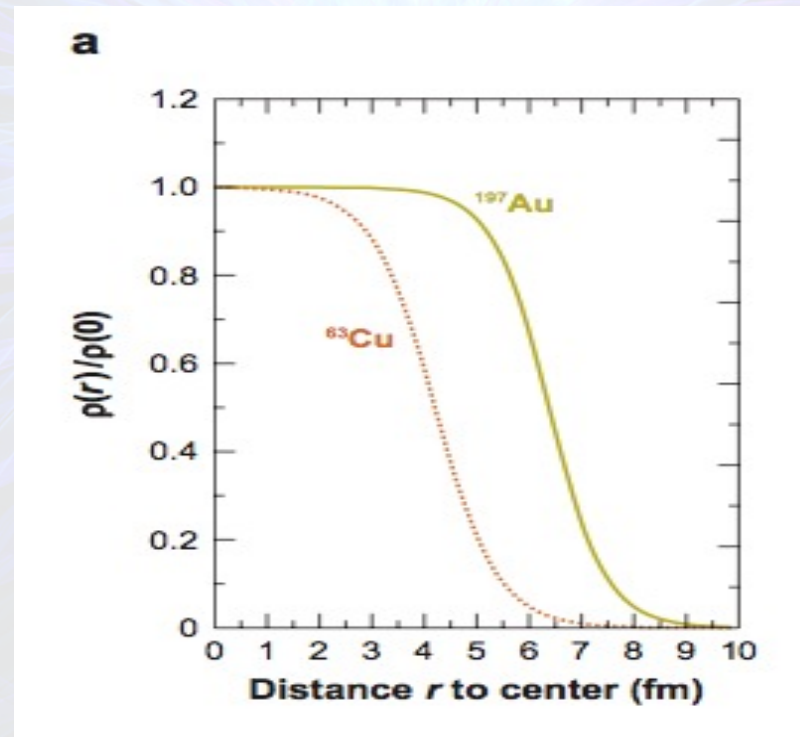
- Event displays





Nuclear Charge Densities

- Charge densities: similar to a hard sphere.
 - Edge is "fuzzy": Woods-Saxon distribution



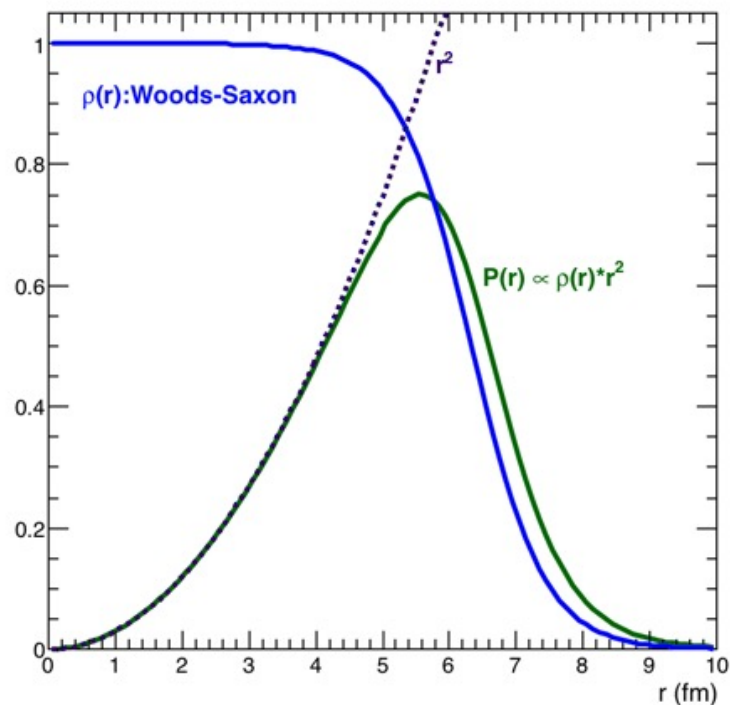
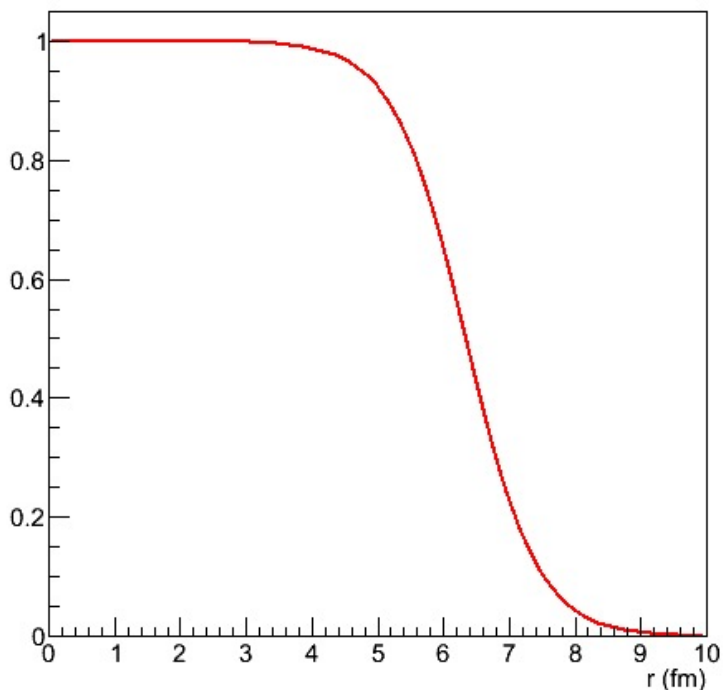


For the Pb nucleus (used at LHC)

- Woods-Saxon density:
 - $R = 1.07 \text{ fm} * A^{1/3}$
 - $a = 0.54 \text{ fm}$
 - $A = 208 \text{ nucleons}$
- Probability : $\propto r^2 \rho(r)$

$$\rho(r) = \frac{\rho_0}{1 + e^{\frac{r-R}{a}}}$$

Pb Radial Volume Density





Glauber model parameters

- PbPb at 5.02 TeV

- Nuclear radius 6.62 ± 0.06 fm
- Skin depth 0.546 ± 0.010 fm
- d_{\min} 0.4 ± 0.4 fm
- σ_{NN}^{inel} 70 ± 5 mb

- <http://dx.doi.org/10.1016/j.softx.2015.05.001>



Nuclei: A bunch of nucleons

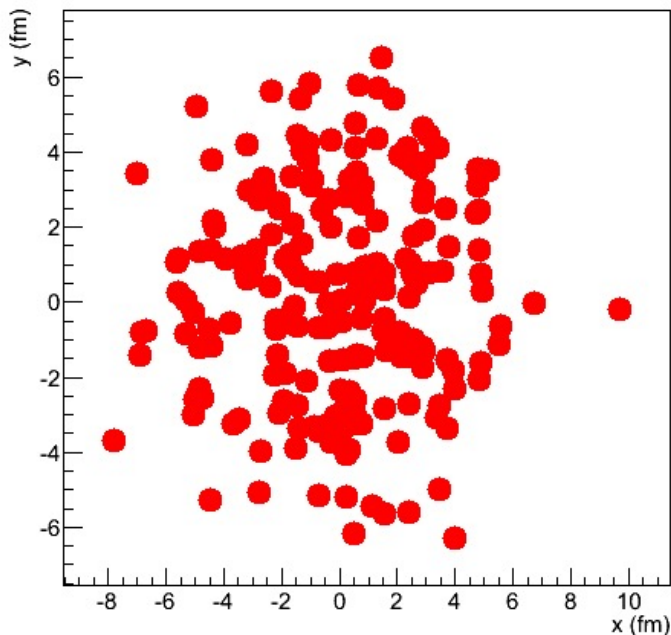
- Each nucleon is distributed with:

$$P(r, \theta, \phi) = \rho(r) dV = \rho(r) r^2 dr d(\cos \theta) d\phi$$

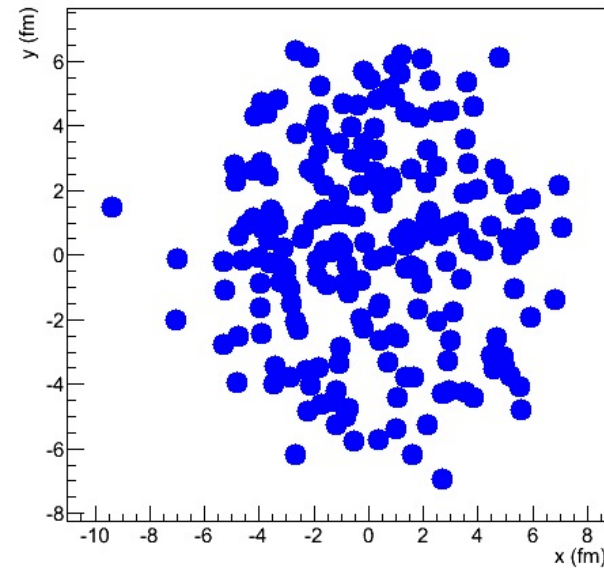
- Angular probabilities:

- Flat in ϕ , flat in $\cos(\theta)$.

Nucleus A



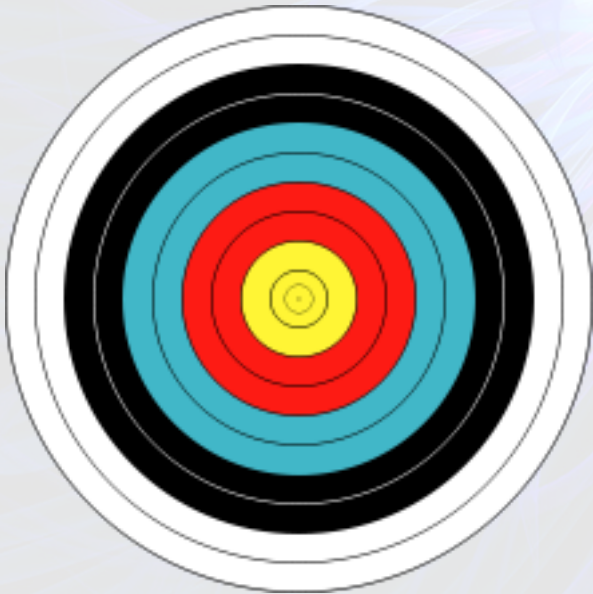
Nucleus B



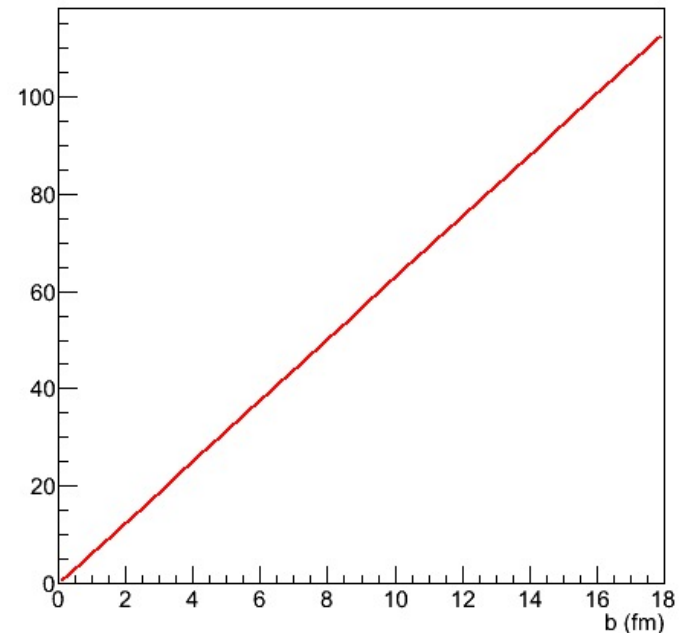


Impact parameter distribution

- Like hitting a target:
- Rings have more area
- Area of ring of radius b , thickness db : $2\pi b db$
- **Area proportional to probability**



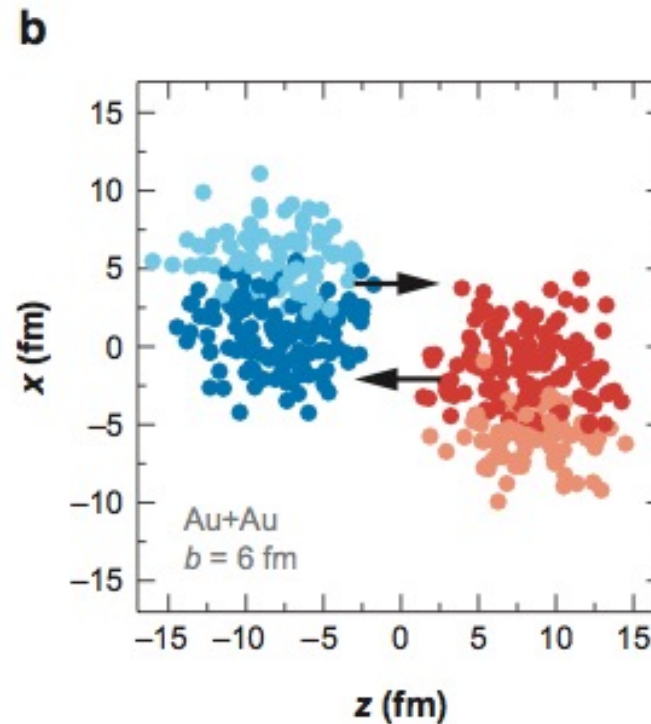
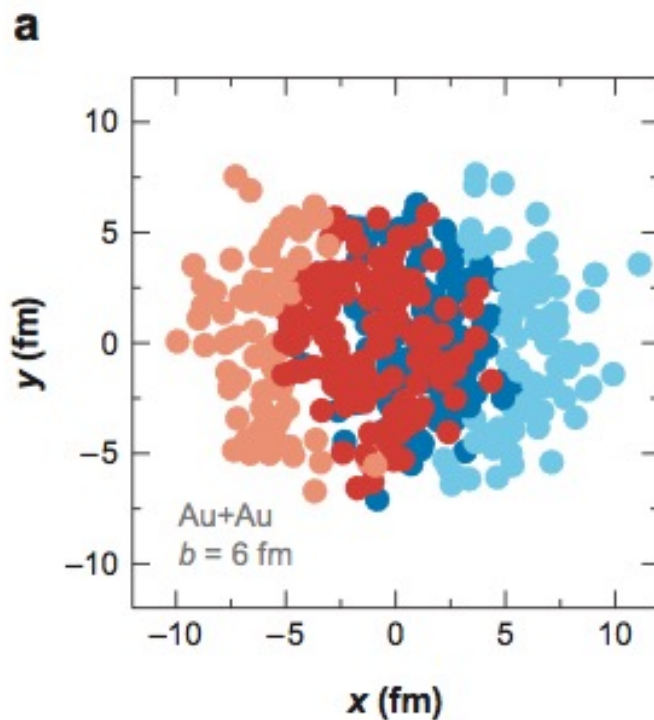
Impact Parameter Probability





Collision:

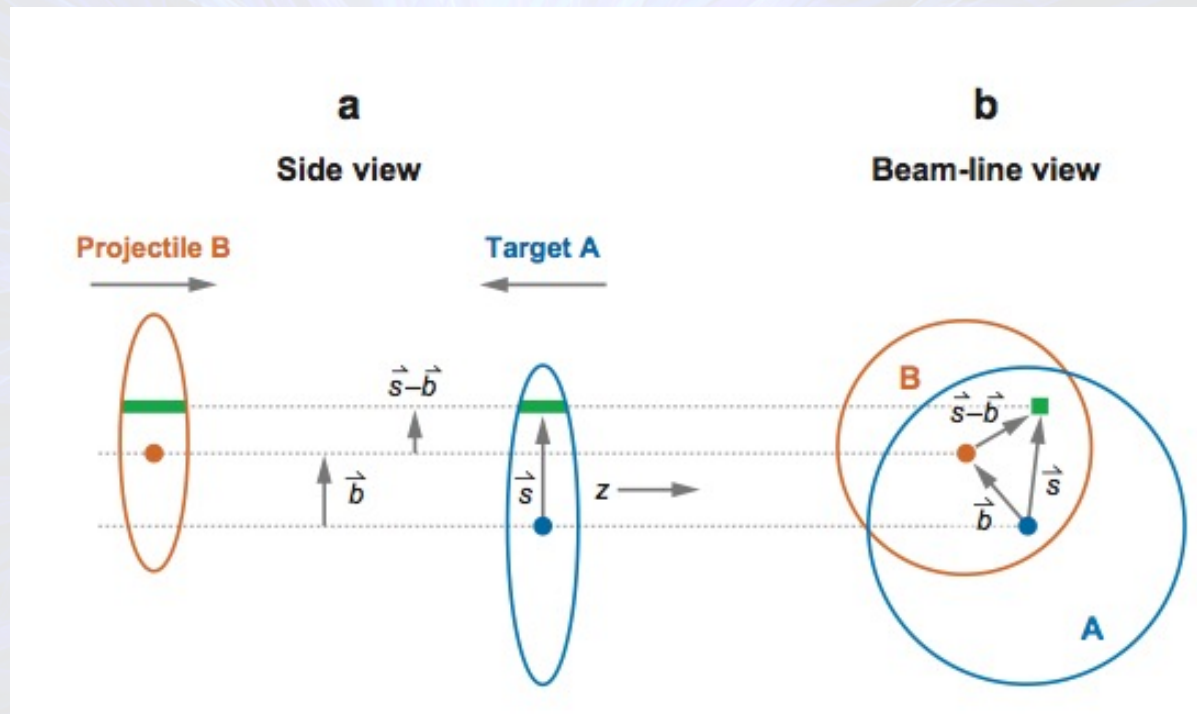
- 2 Nuclei colliding
- Red: nucleons from nucleus A
- Blue: nucleons from nucleus B





Monte Carlo Model of nuclear collisions

- Nuclear Collisions, Glauber model





Monte Carlo Model of Nuclear Collisions

1. Nuclear Density Function

- Make plots of the nuclear density for the Pb nucleus

2. Distribution of nucleons in the nucleus

- Using the nuclear density function, write a function that will randomly distribute A nucleons in the nucleus ($A=208$ for Pb).
- Make a plots of the x-y, and x-z coordinates of the nucleons in sample nucleus.
 - You will need to distribute them in 3D. You can use spherical polar coordinates, then convert to cartesian.



Project: Monte Carlo Model of Nuclear Collisions

3. Impact Parameter, b

- Make a plot of the impact parameter probability distribution
- For $b = 6$ fm, make an example collision between two nuclei. Plot the x-y coordinates of the nucleons in each nucleus.

4. Number of collisions, Number of participants

- For each pair of nucleons (one from nucleus A, one from nucleus B), check if there is a collision.
 - Nucleon-Nucleon Collision:
 - Find the distance d in the x-y plane between each nucleon-nucleon pair (the z axis is the beam axis, see slide 6)
 - Collision: when $d^2 < \sigma/\pi$. Use $\sigma = 65$ mb (where 1 b = 10^{-28} m²).
 - **Any nucleon that collides is called a “participant”. Color each participant a darker color.**
 - **Count the number of nucleon-nucleon collisions.**



Project: Monte Carlo Model of Nuclear Collisions

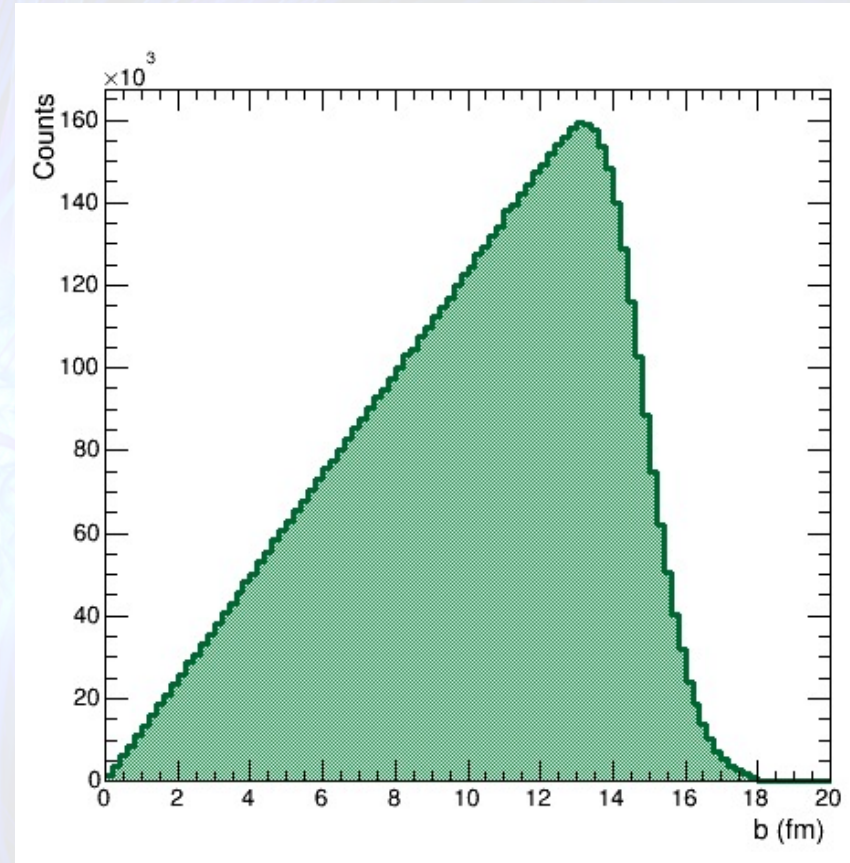
5. Many collisions!

- Simulate 10^6 nucleus-nucleus collision events.
- Draw a random impact parameter from the distribution ($P(b)$ proportional to b).
- Calculate N_{part} , N_{coll} for each collision.
- For those events where there was an interaction ($N_{coll} \geq 1$), fill histograms of
 - the impact parameter, b .
 - the number of participants
 - the number of collisions
- In part II of the project, we will model particle production, and compare it against data.



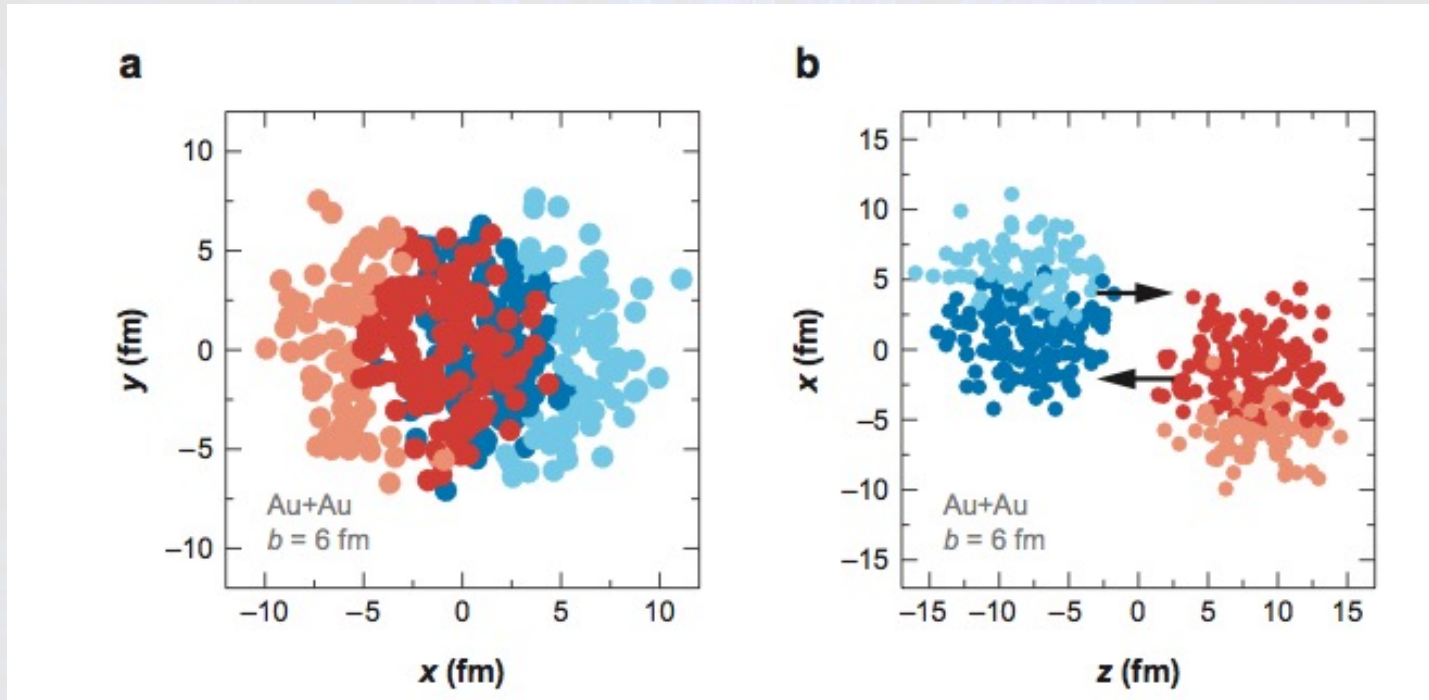
Interaction Probability vs. Impact Parameter, b

- After 10M events
- Beyond $b \sim 2R$ Nuclei miss each other
 - Note fuzzy edge
- Largest probability:
 - Collision at $b \sim 12-14$ fm
- Head on collisions:
 - $b \sim 0$: Small probability





Binary Collisions, Number of participants

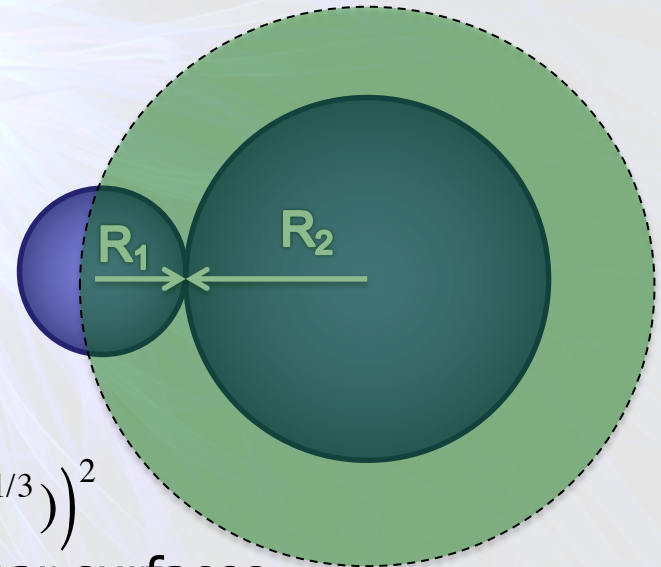


- If two nucleons get closer than $d^2 < \sigma/\pi$ **they collide.**
- **Each colliding nucleon is a “participant” (Dark colors)**
- **Count number of binary collisions.**
- **Count number of participants**



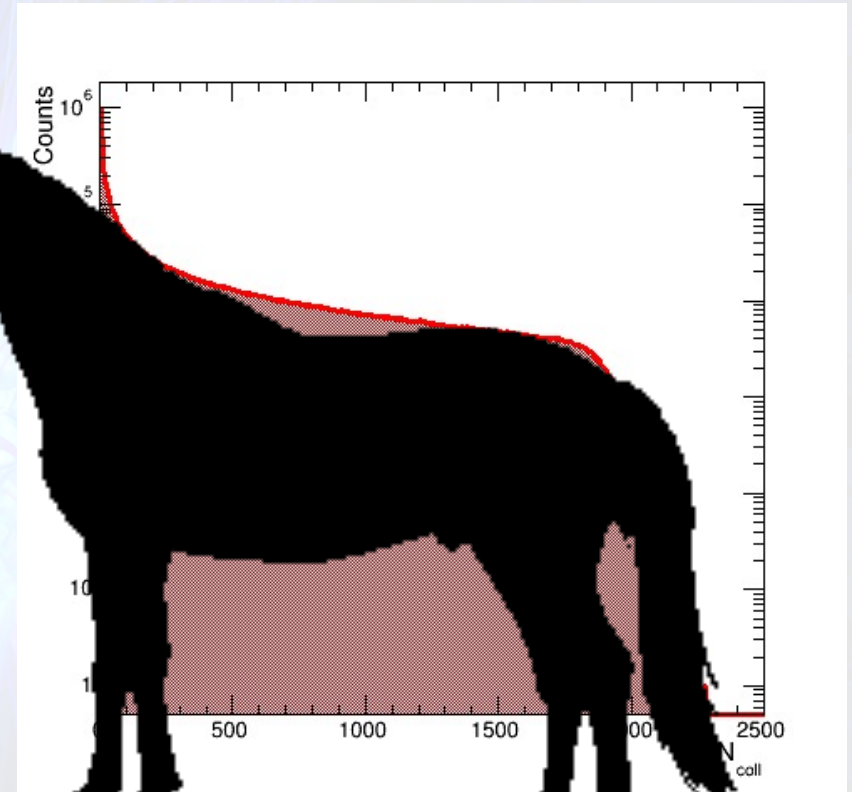
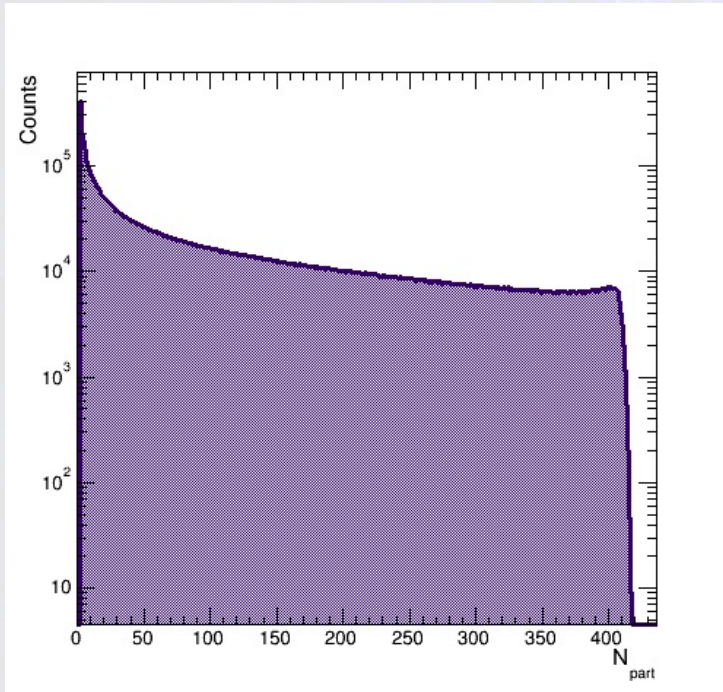
Cross Section in Nuclear Collisions

- Nuclear forces are short range
 - Range for Yukawa Potential $R \sim 1/M_x$
 - Exchanged particles are pions: $R \sim 1/(140 \text{ MeV}) \sim 1.4 \text{ fm}$
 - Nuclei interact when their edges are $\sim 1 \text{ fm}$ apart
 - 0th Order: Hard sphere
 - $\sigma_{\text{geom}} = \pi (R_1 + R_2)^2 = \pi r_0^2 (A_1^{1/3} + A_2^{1/3})^2$
 - $r_0 = 1.2 \text{ fm}$
 - Bradt & Peters formula
 - $\sigma_{\text{geom}} = \pi r_0^2 (A_1^{1/3} + A_2^{1/3} - b)^2$
 - b decreases with increasing A_{min}
 - J.P. Vary's formula:
 - $\sigma_{\text{geom}} = \pi r_0^2 (A_1^{1/3} + A_2^{1/3} - b_0 (A_1^{-1/3} + A_2^{-1/3}))^2$
 - Last term: curvature effects on nuclear surfaces





Find N_{part} , N_{coll} , b distributions

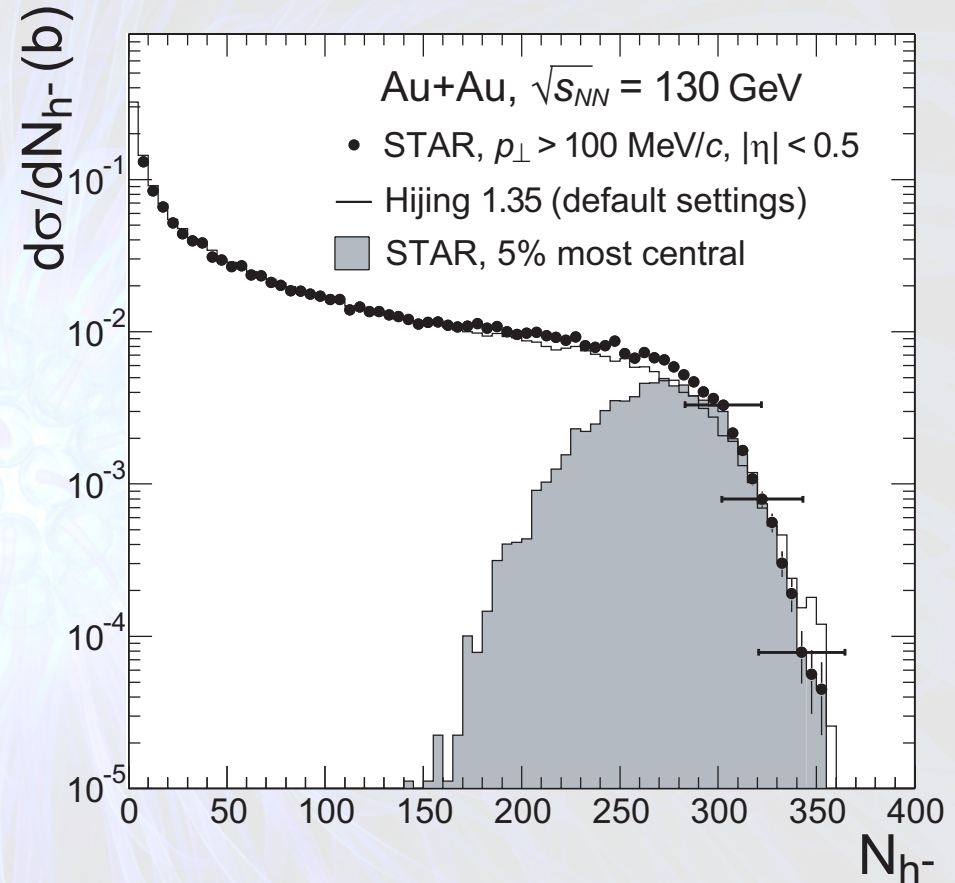
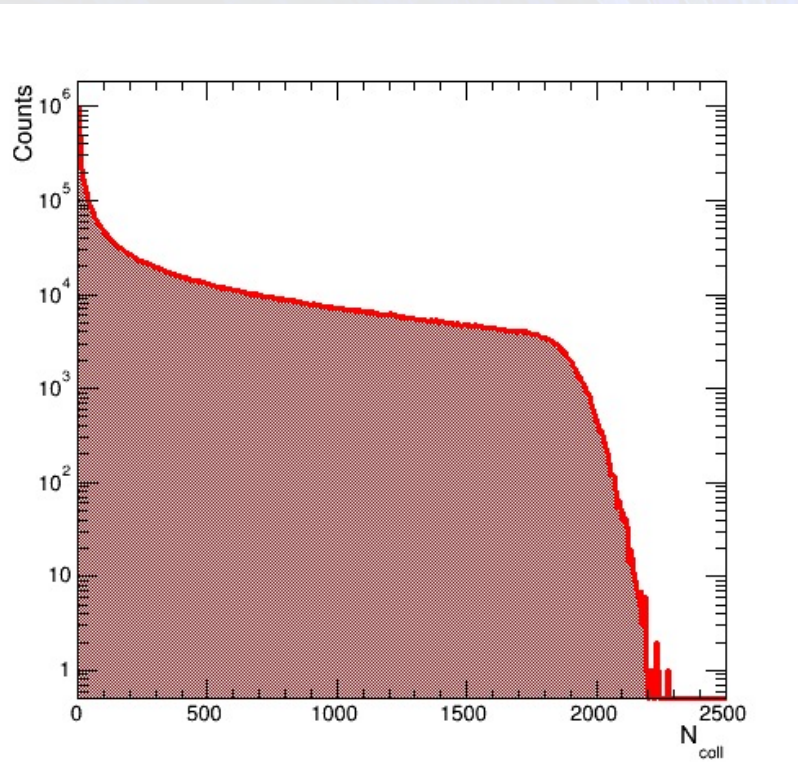


● Nuclear Collisions



From Glauber to Measurements

● Multiplicity Distributions in STAR



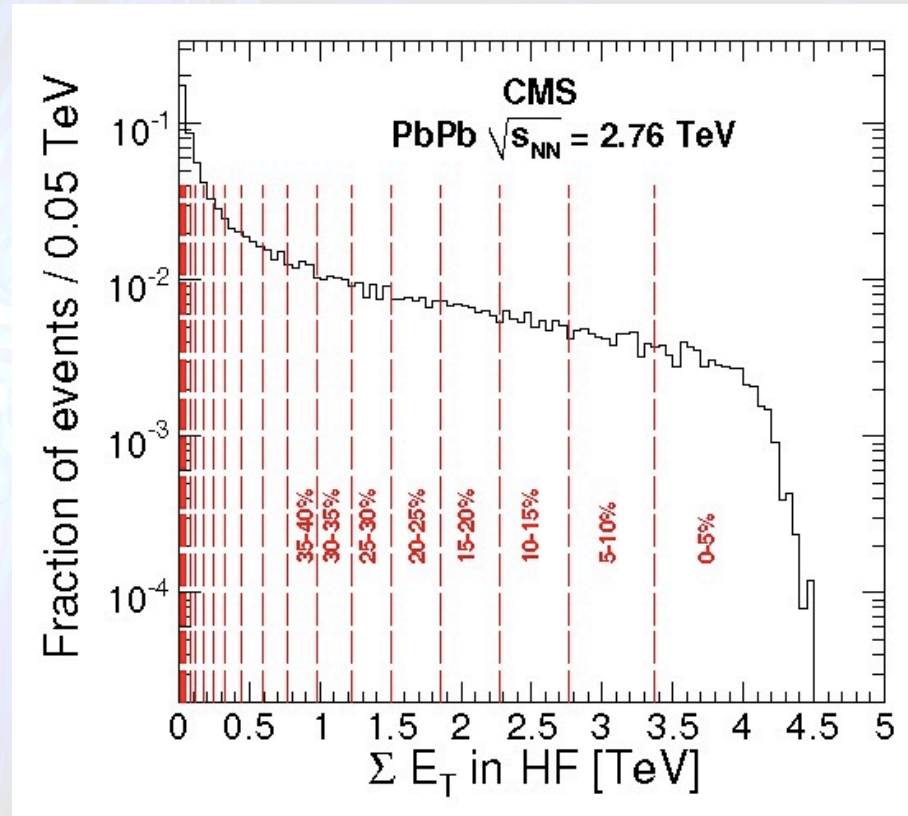
MCBS, Ph.D Thesis

Phys.Rev.Lett. 87 (2001) 112303



Comparing to Experimental data: CMS example

- Each nucleon-nucleon collision produces particles.
 - Particle production: negative binomial distribution.
- Particles can be measured: tracks, energy in a detector.
- CMS: Energy deposited by Hadrons in "Forward" region

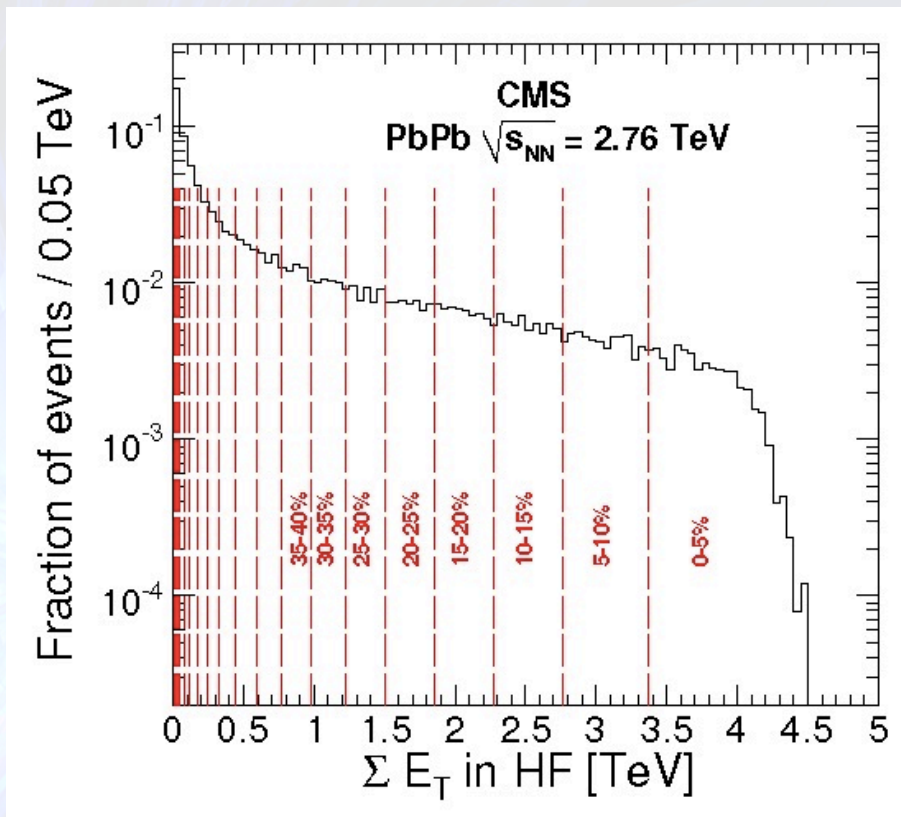




Centrality Table in CMS

- From CMS MC Glauber model.

- CMS: HIN-10-001,
- JHEP 08 (2011) 141



Centrality	0-5%	5-10%	10-15%	15-20%	20-25%	25-30%
N_{part}	381 ± 2	329 ± 3	283 ± 3	240 ± 3	203 ± 3	171 ± 3
Centrality	30-35%	35-40%	40-45%	45-50%	50-55%	55-60%
N_{part}	142 ± 3	117 ± 3	95.8 ± 3.0	76.8 ± 2.7	60.4 ± 2.7	46.7 ± 2.3
Centrality	60-65%	65-70%	70-75%	75-80%	80-85%	85-90%
N_{part}	35.3 ± 2.0	25.8 ± 1.6	18.5 ± 1.2	12.8 ± 0.9	8.64 ± 0.56	5.71 ± 0.24